

University of Cihan-Sulaimaniya
Engineering Faculty
Architectural Engineering Department



ENGINEERING MECHANICS

Chapter 5: Equilibrium of Rigid Body

2nd Grade- Fall Semester 2024-2025

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Communitising Technology

Chapter Description

- **Aims**
 - To transform the rigid body into free-body diagram
 - To apply the equation of equilibrium in the rigid body
- **Expected Outcomes**
 - Able to determine the forces involved in the rigid body using equation of equilibrium
- **References**
 - Russel C. Hibbeler and Kai Beng Yap (2013) Engineering Mechanics: Statics & Dynamics, 13th Edition

Chapter Outline

1. Introduction of Equilibrium
2. Free-Body Diagrams
3. Equations of Equilibrium
4. Example Calculation



1.1 Introduction of Equilibrium

What is equilibrium?

A body is in the static motion, not move, not rotate, or moving with constant velocity

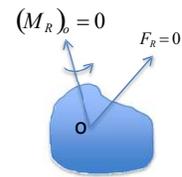
A body exposed to the 3 forces there are:

- 1) External Force
 - 2) Couple moment system
 - 3) Internal Force
- } Affected by gravitational, electrical, magnetic, or contact force caused by adjacent bodies
→ Interaction between particles within the bodies

Equilibrium equation of a body at point O:

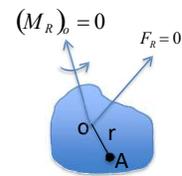
$$F_R = \sum F = 0 \quad (\text{zero})$$

$$(M_R)_o = \sum M_{F_R, o} = 0 \quad (\text{zero})$$



Equilibrium equation of a body at point A:

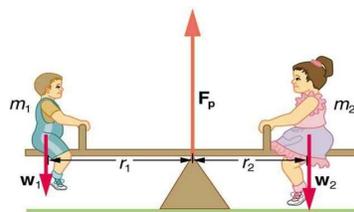
$$\sum M_A = r \times F_R + (M_R)_o = 0$$



5.2 Free-Body Diagrams (FBDs)

What is FBDs?

1. Sketch all the forces and couple moments surroundings apply on a body.
2. Primary importance to solve the problems in mechanics

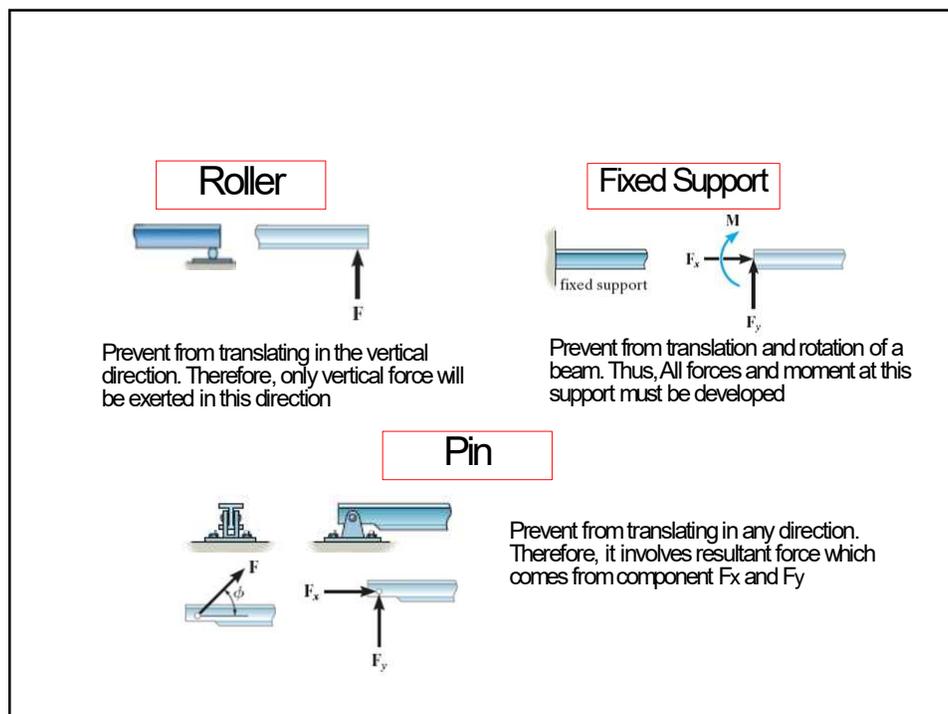


Source: <https://www.boundless.com>

5.2 Free-Body Diagrams

Support Reactions:

- 1) Force caused by the supports and points which contacted to body subjected to coplanar force systems
- 2) If a support prevents the translation of a body in a given direction, means that a force is developed on the body in that direction
- 3) If rotation is prevented, a couple moment exerted on the body



Procedure of FBDs:

- 1) Draw the outline of body shape
- 2) Indicate all dimensions of the body
- 3) Allocate all forces and couple moments act on the body
- 4) Label their magnitudes and directions

Example**Problem:**

Draw the FBDs for the Figure below:

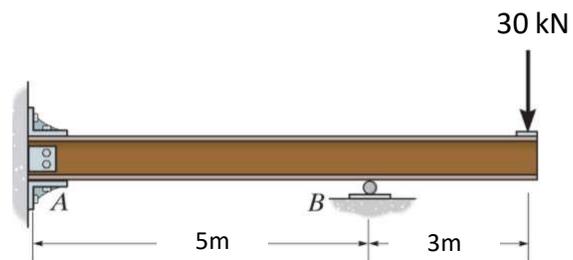


Figure 1: Fixed beam

Source: <http://www.chegg.com>

Example Solution:

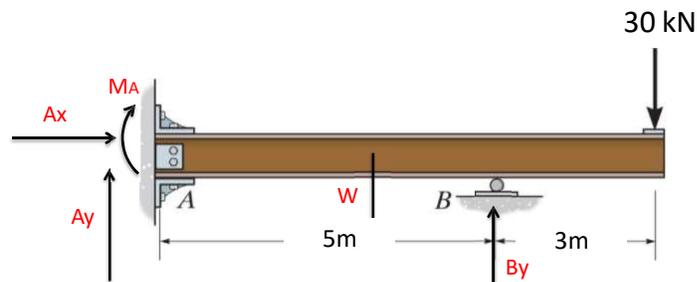


Figure 1: Fixed beam

Source: <http://www.chegg.com>

5.3 Equations of Equilibrium

- For equilibrium of a rigid body in 2D,

$$\sum F_x = 0$$

$$\sum F_y = 0$$

$$\sum M_O = 0$$

- $\sum F_x$ is sum of all forces in x-axis
- $\sum F_y$ is sum of all forces in y-axis
- $\sum M_O$ is sum of the couple moments and moments of forces due to point origin (o)

Procedure of Equilibrium Equation:

- 1) After draw FBDs, apply equation of equilibriums

$$\sum F_x = 0$$

$$\sum F_y = 0$$

$$\sum M_O = 0$$

- 2) For the moment at point O, all the forces must be considered and sign of the moment based on the rotation
- 3) Use 3 equilibrium equations in determining third unknown
- 4) Negative result shows the direction of the determined force in opposite

**EXAMPLE
CALCULATION**

Example Problem

1:

Determine the horizontal and vertical components of reaction on the beam as shown in Figure 2 below:

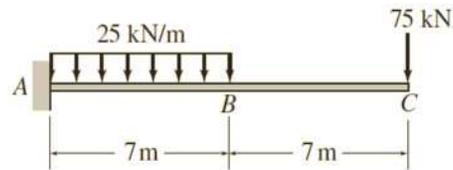


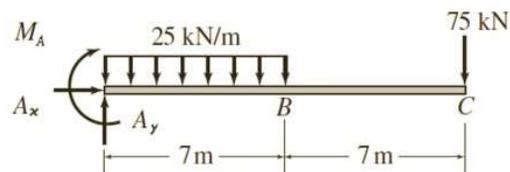
Figure 2: Beam with load



http://www.engineeringwiki.org/wiki/Beam_Virtual_Work

Solution:

1) FBDs



http://www.engineeringwiki.org/wiki/Beam_Virtual_Work

2) Find the force at support system using equilibrium equation

Answer: $A_x = 0 \text{ kN}$, $A_y = 250 \text{ kN}$, $M_A = 1662.5 \text{ kN}$



http://www.engineeringwiki.org/wiki/Beam_Virtual_Work

Conclusion of The Chapter 5

- Conclusions
 - The FBDs diagram have been introduced and applied to solve the equilibrium problems for the rigid body





•Thank you