Cihan University-Sulaymaniyah



Financial Mathematical

Department of:

Accounting

Stage-ONE

Prof.Dr. Obaid Mahmmood Mohsin

Academic Year: 2023/2024



[DOCUMENT TITLE]

[Document subtitle]

2023-2024

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MODULE DESCRIPTION FORM

	Module Information							
Module Title	Financial Math	ematics						
Module Type	Degree				Theory			
Module Code					 □ Lecture □ Lab □ Tutorial □ Practical 			
Language	English							
ECTS Credits					☐ Fractical ☐ Seminar ☐ Report ☐ Extra activity			
Module Level			Semester o	f Deliver	2 nd Semester			
Administering Dep	partment	Accounting	College Administration and Finance			ance		
Lecturer	Dr. Obaid Mah	mmood Mohsin						
Academic Title		Professor	Qualificatio	ication PHD. Sta				
Module Tutor	Dr. Obaid Mal	nmmood Mohsin	e-mail	il Obaid.mohsin808@gmail.co		il.com		
Peer Reviewer Name			e-mail					
Scientific Committee Approval Date			Version Number					
Cycle of Study		Bachelor	Form of Education		Full time			

Relation with other Modules								
Prerequisite module		Semester						
Co-requisites module		Semester						

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Cihan University Sulaimaniya? College of Administration & Finance......

Department: ...Accounting......

Discipline:

Stage: 1st stage

Total Contact Hours:	25
Total Self Study Hours:	56
Total No. Hours:	81
ECTS:	3



		Contact Hours					Self-Study					
N	No. of Weeks	Theoretical	Practical	Lab	Project	Visit	Quiz	Reading	Assignment	Report	Midterm Exam.	Final Exam.
1 ^s	t Week											
(Registration)	-	-	-	-	-	-	-	-	-	-	-
2ª	^{1d} Week	1						1				
31	rd Week	1	1					1				
4 ^t	^h Week	1	1				2	1				
5 ^t	^h Week	1	1									
6 ^t	^h Week	1	1					1	2	2		
7 ^t	^h Week	1	1				2					
8 ^t	^h Week	0	2					1			12	25
9 ^t	^h Week	1	1									
1	Oth Week	0	2					1				
1	1 th Week	1	1									
1	2 th Week	0	2						2			
1	3 th Week	1	1				2					
1	4 th Week	1	1					1				
	15th Week											
(Final Exam.											
	16th Week											
	Final Exam.)											
Τ	OTAL	10	15				6	7	4	2	12	25

Delivery Plan (Weekly Syllabus)						
	Material Covered					
Week 1	Chapter One Simple Interest Interest InterestDefinition and elements. Examples					
Week 2	The types of Interest How to find Simple interest Examples					
Week 3	The Amount in Simple interest: Calculate the period: Examples					
Week 4	Types of Simple Interest: Standard interest Commercial interest—and- Exact interest The Relationship between Commercial Interest & Exact Interest: Examples					
Week 5	The difference between Commercial Interest & Exact Interest: The Numbers Method: Examples					
Week 6	Problems & solutions					
Week 7	Mid-Term Exam					
Week 8	Chapter Two Commercial discount with simple interest. The concept of trade discount. Definition of trade discount. Examples					
Week 9	Trade discount account The normal Method: The Constant denominator method Current value of a commercial paper Examples					
Week 10	Rational (Correct) Discount Examples					
Week 11	Problems & solutions					
Week 12	Chapter Three Compound Interest					

	Compound Interest Effective Rate of Interest: Examples
Week 13	The actual interest on simple interest rate that is equivalent to compound interest rate is called the effective rate. Depreciation: The straight -line method - The Constant -Percentage Method Examples
Week 14	Problems & solutions
Week 15	Preparatory Week
Week 16	Final Exam

	Delivery Plan (Weekly Lab. Syllabus)
	Material Covered
Week 1	
Week 2	
Week 3	
Week 4	
Week 5	
Week 6	
Week 7	
Week8	
Week9	
Week 10	
Week 11	
Week 12	
Week 13	
Week 14	
Week 15	
Week 16	

Module Aims, Learning Outcomes and Indicative Contents								
Module Objectives	Sophisticated mathematical models, whose solution often requires computers, are important in finance. This course will give students the basic numerical tools and practice solving financial problems on computers. students will be expected to implement basic algorithms in a high-level programming language.							
Module Learning Outcomes	On completion of this course, students should be able to 1-given any two of interest rate, present value, or future value, calculate .the third based on simple interest 2-Given any one of the effective interest rates, the nominal .interest m-they, or the force of interest, calculate all of the other items 3-Write the equations of value given a set of each flow and interest rate							

Learning and Teaching Strategies							
Strategies	Whiteboard, whiteboard maker, data show, course note. Assessment scheme.						

	Module Evaluation									
Assessm	ent Types	Time/Number	umber Weight (Marks)		Relevant Learning					
				Week Due	Outcome					
	Quizzes	5/3	15	4,7,13						
Formative	Assignments	2/5	10	6,12						
assessment	Projects /	1/5	5	6						
	Report									
Summative	Midterm Exam	2hr	20	8						
assessment	Final Exam	3hr	50	15						
Total assessme	ent	•	100% (100 Marks)							

Learning and Teaching Resources							
	Text	Available in the Library?					
Required Texts	Financial math. By Dr. Clarence H. Richardson. Mastering Financial mathematics by Alastair Iday						
Recommended Texts	Lectures gave to students						
Websites							

Grading Scheme مخطط الدرجات							
Group	Grade	التقدير	Marks %	Definition			
	A - Excellent	امتياز	90 - 100	Outstanding Performance			
Success Group	B - Very Good	جيد جدا	80 - 89	Above average with some errors			
	C - Good	جيد	70 - 79	Sound work with notable errors			
(50 - 100)	D - Satisfactory	متوسط	60 - 69	Fair but with major shortcomings			
	E - Sufficient	مقبول	50 - 59	Work meets minimum criteria			
Fail Group	FX – Fail	راسب (قيد المعالجة)	(45-49)	More work required but credit awarded			
(0 – 49)	F – Fail	راسب	(0-44)	Considerable amount of work required			

Note: Marks Decimal places above or below 0.5 will be rounded to the higher or lower full mark (for example a mark of 54.5 will be rounded to 55, whereas a mark of 54.4 will be rounded to 54. The University has a policy NOT to condone "near-pass fails" so the only adjustment to marks awarded by the original marker(s) will be the automatic rounding outlined above.

Approved by Head of the Branch / Department		
Signature		
Date	6/3/2024	
Name	Ass Prof. Dr.Munadhil Abd-Aljabar	

Approved by Curriculum Development Committee and Bologna Process Committee

Signature	
Date	
Name	

Chapter One

Simple Interest

<u> 1- Interest:</u>

Interest is the core of the business and financial activities in our business life, in banks, insurance companies and others financial institutions.

Depending on some sources, the lending of "food money" was commonplace in Middle Eastern civilizations as early as 5000 BC. The argument that acquired seeds and animals could "reproduce themselves" was used to justify interest. All religions consider it charging of interest (Riba).

The first attempt to control interest rates through manipulation of the money supply was made by the Banque de France in 1847, continuous till this day and consider it as an " Investment ".

Before we enter into the main subject " Interest ", we must first know some simple things, and why there is interest.

Every one of us have income; daily or monthly, spending of this income depending on our expenses and consumptions (foods, drinks, clothes, transportations ... etc.).

The income formula is.

Y = C + S

where:

Y = income

C = consumption

S = saving

Some of us may have high-income with normal expenditures, so that will make some money for saving, day by day or month by month.

This will make a saving moneys increase in our house, more of us will be afraid on his moneys from (fire, steal), some of us thinking about investments to increase them and keep safety.

For these reasons we think to saving them in banks or other financial institutes:

1) To keep them safety.

2) To invest and increase them.

So that the income formula will be,

$$\mathbf{Y} = \mathbf{C} + \mathbf{I}$$

where: I = investing. On the other side, there are some people need moneys to building house, to buy a new car or even to do business ... etc.

So that both of these two people go to the banks, one is to save his money in it by deposit, and the other to get a loan from the bank.

Banks: are A legal intermediary that transfers the savings of individuals, businesses, and governments into loans or investments.

For example, we suppose that Mr. (Z) has surplus money (\$ 10000), he want to keep it safe and increase it, so he will take his money and deposit it in the bank (B); for (1) year at interest rate (10%).

After that Mr. (K) needs a sum (\$ 10000) to buy a car, he will go to the bank (B) and get a loan for this sum, for (1) year at interest rate (12%).

After (1) year, Mr. (K) will back to the bank (B) a sum (11200), then the Bank will back to Mr. (Z) a sum (11000), the profit of bank was (200)

2- Interest ... Definition and elements.

Now we have an imagining about the "Interest ", so we can define the Interest: " *as A fee that is charged by a lender to a borrower for the right to use the borrowed funds.* ", this fund we call them " Capital. Capital: *is one of the production elements.*

The interest is consisting of three elements:

1– The principal (P): is a sum that will be used by others through borrowing it for specified period. May be from person to bank, or bank to person, or any other form.

2-Number of periods (n): is the periods of using money by others; may be days, months, or years, and must be specific.

3 – Rate of interest (r): is the price of interest that will be agreed on between the two sides, credit and debit. It measures as (100) units per year, if there is no agreement for another deal.

3- The types of Interest

We have two types of interest:

Simple Interest

and

Compound Interest.

The simple interest is calculating each year by itself without adding any sums (one year usually),

the compound interest; calculate for first year as simple interest, and for another year adding the interest year by year (we will explain about later).

4- Simple interest

Simple interest is a quick method of calculating the interest charge on a loan.

Simple interest usually calculating for one year or less than that, it consists of three elements:

1) Principal (original sum).

2) Number of periods (days, months or year).

3) Rate of interest (the price of interest; percentage).

The formula that uses to calculate the simple interest is:

I =P. n. r.

when.

I = Interest.

P = Principal (original sum).

n = number of periods.

r = rate of interest (%)

Now we will take several examples to explain how it is working,

Ex. 1: A man have a sum 1000 ID, he wants deposit it in a bank for (1) year, with rate of interest (10 %). Find the interest (simple interest) for him at the end of period.

Sol.

P = 1000 ID, n = 1 year, r = 10 %, I = ? I = P. n. r I =1000 *1 *(10/100) I = (1000 *1 *10)/100 I =100 ID

Ex. 2: Mr. Anmar wants to invest a sum 2400 ID for three years, in Cihan bank with interest rate (13 %). Find the interest at the end of year three?

Sol.

P = 2400 ID, n = 3 years, r = 13 %, I = ? I = P. n. r I = 2400 *3 *(13/100) I = (2400*3 *13)/100 I = 936 ID

Ex. 3: Find interest of a sum 3060 \$ for (6) years at (8%)?

Sol.

```
P = 3060 $, n = 6 years, r = 8%, I =?
```

l = P. n. r

I =3060 *6 *(8/100)

I = (73060 *6 *8)/100

I =1468.8\$

Ex. 4: Cihan bank pay interest rate (9 %) for saving account, if a business man have 560400 ID and he want to invest it for (4) years. Find the interest?

Sol.

P = 560400 ID, n = 4 years, r = 9 %, I =?

I = P. n. r

I =560400 *4 *(9/100)

I = (560400 *4 *9)100

I =201744 ID

In the case of calculating the interest by months, we must dividing the number of periods (n) on (12) months , because it less than one year.

Here are examples,

Ex. 5: Ahmed have a sum 180000 ID, he want to deposit it in Iraqi investment bank for (8) months, at rate of interest (12 %). Find the interest.

Sol.

P = ID 180,000, n = 8 months, r = 12 %, I =?

I = P. n. r

I = P * (n/12) * (r/100)

I =180000 *(8/12) * (12/100)

I =(180000 *8 *12)/(12 *100)

I =14400 ID

Ex.6: Find the interest of 102036 \$ for (11) months at rate of interest (11%).

Sol.

P = 102036 \$, n = 11 months, r = 11 %, I = ? I = P. n. r I = P *(n/12) *(r/100) I = 102036 *(11/12) *(11/100) I = (102036 *11 *11)/ (12 *100) I = 10288.63 \$

Ex-7: Calculate the interest for a student want to keep here money in Cihan Bank for (10) months , she have $7655.38 \pm$ and the interest rate in the bank is (1.5) %.

Sol.

P = 7655.38£, n = 10 months, r = 1.5 %, l = ? I = P. n. r I = P* (n/12) * (r/100) I = 7655.38 *(10/12) *(1.5/100) I = (7655.38 *10 *1.5)/(12*100) I = 95.692 £

5- The Amount in Simple interest:

The amount value is the principal added to it the interest of the principal that will invest at the end of period, so that the real sum anybody will keep or invest sum's own will receive at the end of period the whole sum, principal and interest together.

Amount = Principal + Interest

A = P + I

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We can also derive this formula; to find direct formula to calculate the amount.

A = P + I

 $A = P + (P^* n^* r)$

common factor [P]

 $A = P (1 + (n^* r))$

Here are examples,

Ex-8: A man deposit 30000 ID in a bank for (4) years , and the rate of interest is (11%). Find the Amount that he will get at the end of year (4).

Sol.

P = 30,000 ID, n = 4 years, r = 11 %, I = ?, A = ?

1) At the beginning, we find the value of interest.

I =P *n *r I =30000 * 4 *(11/100) I = 30000 (4 *(11 /100)) =30000(11/25)=1200 *11 I =13200 ID

2) Then we find the amount that a man will receive at the end of year (4).
 A =P +I
 A =30000 +13200

```
A =43200 ID
```

Or 3- we can find A in one step A = P (1 +(n*r)) A =30000 (1 +(4 * (11/100)) = 30000(1 +11/25) = 30000 (36/25) A=1200 *36 =43200 ID

Ex-9: Mr. Ali wants to keep his sum 108788.5 \$ in a bank for (8) months, and the rate of interest of the bank is (15%). Find his balance?

Sol. P = 108788.5 \$, n = 8 months, r = 15 %, I =?, A =?

Here we will use the direct way to find the amount by this formula:

```
A = P. (1 +(n *r))
A =108788.5 *[1 +(8/12)*(15/100)]
A =108788.5 * [1+(8*15)/(12 *100)]
A =108788.5 * [1+(120/1200)]
A =108788.5 * [1+(0.1)]
A =108788.5 *[1.1]
A =119667.35 $
```

Ex-10: Find the amount of sum 160585.35 ID for (15) months, at (13%))? Sol. P = 160585.35 ID, n = 15 months, r = 13%, A =? A = P *(1 + (n *r)) A = 160585.35 *[1+(15/12) *(13/100)] A = 160585.35 * [1 + ((15/12) *(13/100)] A = 160585.35 * [1 + (15*13)/(12 *100)] A = 160585.35 * [1 + (195/1200)] A = 160585.35 * [1 + (0.1625)] A = 160585.35 * [1.1625] A = 186680.47 ID

6- Calculate the period:

The financial activities in banks usually do every day ; deposit , withdraw or discount , etc. So, we need in this case to calculate the period by days.

In the commercial activates usually depend on standard Time of period as (360) days by one year ; it is mean (30) days for every month. There is also Real time of period as (365 or 366) days by one year ; it is mean (30 or 31 or 29 or 28) days for every month. The following table, can explain and simple the way of calculating:

No.	Name	Short	Days
1 -	January	Jan.	31
2 -	February	Feb.	28 or 29
3 -	March	Mar.	31
4 -	April	Apr.	30
5 -	May	May	31
6 -	June	June	30
7 -	July	July	31
8 -	August	Aug.	31
9 -	September	Sept.	30
10 -	October	Oct.	31
11 -	November	Nov.	30
12 -	December	Dec.	31

To calculate the period of days we must:

1 – Don't use the first day of deposit.

2 – Use the last day of withdraw.

3 – Calculate the days of months between deposit and withdraw.

To explain more, we will take some examples:

Ex-11: Find the period between 1st March to 20th May? Sol.

	March	\rightarrow	April →	May
31			30	**20
	* 31 – 1	l	30	20
30	+	30	+	20 = 80 days

* Subtract days of all months from the day of deposit.

** the last month, we just use the date till to withdraw

money; not all the days of month

Ex -12: Calculate the number of days between 22nd May to 14th Sep.

Sol.

May →	June →	July →	Aug. →	Sep.
31	30	31	31	14
31 - 22	30	31	31	14

9 + 30 + 31 + 31 + 14 = 115 days

7- Types of Simple Interest:

There are three types of simple interest:

1) Standard interest : this type of interest calculate by dividing the number of periods (n) on (360) days ,

which represents every month by (30) days.

 $S(I) = P^{*}(n/360) * (r/100)$

when,

S = standard interest

2- Commercial interest: this type of interest is also calculated by dividing the number of periods (n) on (360) days , which represent every month by (30) days.

Com.(I) =P *(n/360) *(r/100) when ,

Com. (1) = commercial interest

3- Exact interest : this type of interest is calculated by divide the number of periods (n) on (365 or 366) days , which represent the days of whole year. Ex.(I) =P *(n/360 or 366) *(r/100)

when,

EX. (I) = Exact interest

We notice that the standard and commercial interest are the same in the way of calculation, so for that we depend on commercial interest in our financial activities.

Ex-13: Mr. Kamal want to invest his sum 36000 ID for (100) days in Trade Bank of Iraq, the rate of interest is (12 %). Find commercial interest.

```
Sol.
P = 36000 ID, n = 100 days, r = 12% , Com. (I) = ?
```

```
Com .(I) =P *(n/360) *(r/100)
Com .(I) = 36000 * (100/360) *(12/100)
Com. (I) =(36000 *100 *12 )/(360 *100)
Com.(I) = 1200 ID
```

Ex-14: Cihan bank pay interest rate (9%) for investing sum, a man have 146800 ID want to invest it for (187) days. Calculate the commercial interest he will gain.

Sol.

```
P = 146800 ID, n = 187 days, r = 9%, Com. (I) = ?
Com(I) =P *(n/360) *(r/100)
Com.(I) = 146800 * (187/360) *(9/100)
Com ,(I) = (146800 *187 *9)/ (360 * 100)
Com .(I) = 6862.9 ID
```

Ex-15: A merchant wants to invest his sum 100,640 \$ for 300 days, and Cihan bank pay (14 %). Find commercial interest?

```
Sol.

P = 100640 ID, n = 300 days, r = 14%, Com. (I) = ?

Com (I) =P *(n/360) *(r/100)

Com.(I) =100640 * (300/360) *(14/100)

Com.(I) = (10040 *300 *14)/(360 *100)

Com. (I) =(422688000/36000)
```

Com.(I) =11741.33 ID

Ex-16: Find the commercial interest of sum 90830 ID , if you know that Cihan bank pay (15%), for 256 days?

Sol.

P = 90,830 ID, n = 256 days, r = 15%, Com. (I) = ? Com. (I) = P *(n/360) * (r/100) Com. (I) = 90830 *(256/360) *(15/100) Com. (I) = 348787200 /36000 Com. (I) = 9688.53 ID

Ex-17: A man want to invest a sum 7432 ID for 169 Days at (10%). Find the Exact interest.

Sol. P = ID 7,432, n = 169 days, r = 10%, Ex. (I) = ? Ex.(I) =P *(n/360)*(r/100) Ex.(I) =7432 *(169/365) * (10/100) Ex.(I) =(7432 *169 *10)/36500 Ex.(I) =12560080/36500 Ex.(I) =344.11 ID

Ex-18: Cihan bank pay (14%) as rate of interest , if you think to invest a sum 288500 ID for (135) days ; how much will be the Exact interest you will receive ?

Sol.

P = 288,500 ID , n = 135 days , r = 14% , Ex. (I) = ? Ex.(I) =P *(n/365) *(r/100) Ex.(I) =288500 *(135/365) *(14/100) Ex.(I) =(288500 *135 *14)/(36500) Ex.(I) =545265000/36500

Ex.(I) =14938.76 ID

Ex-19: A man want to invest his money in Trade Bank of Iraq (TBI) for 201 days, and the rate of interest is (9%) for 86340 ID he want to invest. Calculate exact interest?

```
Sol.

P = 86340 ID, n = 201 days, r = 9%, Ex. (I) = ?

Ex(I) = P *(n/365)*(r/100)

Ex(I) = 86340 * (201/365) * (9/100)

Ex(I) = (86340 *201 *9)/36500

Ex(I) = 156189060 /36500

Ex(I) = 4279.15 ID
```

Ex-20: How much will be the Exact interest if a merchant want to invest his sum 165218\$ for 364 days at (10 %) ? Sol.

P = 165218 ID , n = 364 days , r = 10% , Ex. (I) = ?

```
Ex (I) = P *(n/365) * (r/100)
Ex (I) = 165218 *(364/365) *(10 /100)
Ex (I) = (165218 *364 *10)/36500
Ex (I) = 601393520/36500
Ex (I) = 16476.53 ID
```

<u>8- The Relationship between Commercial Interest & Exact</u> Interest:

We can find any of (Commercial or Exact) Interest in terms of Other, if we look at the equation of each of them:

Com(I) =P *(n/360) *(r/100)

Ex.(I) =P * (n/365) *(r/100)

```
The difference is just in the period, the
Com. (I) = 360 and Ex. (I) = 365,
if we divided the equations.
```

Com.(I) /Ex.(I) = (P *(n/360) *r/100))/ (P *(n/365) * (r/100)) Com.(I) /Ex.(I) = 365/360 Com (I) /Ex.(I) =73/72

Either, Com.(I) = Ex.(I) *73/72 Or Ex.(I) = Com.(I) *72/73

<u>9- The difference between Commercial Interest & Exact</u> Interest :

The difference between the commercial interest and exact interest can be calculate by using the formula:

Diff =Com.(I) -Ex.(I)

one can cross-multiply to get either;

Ex. (I) = 72*Diff Or Com.(I) = 73 *Diff

here are examples,

Ex-21: How much will be the Commercial Interest, if the Exact interest is ID 7200 ?

Sol.

Com.(I) = Ex. (I) * 73/72

Com.(I) = 7200 *73/72

Com.(I) =(7200 *73)/72

Com.(I) = 7300 ID

Ex-22: Find the Exact Interest, when the commercial interest is \$ 3420? Sol.

Ex.(I) = Com. (I) *72/73

Ex.(I) = 3420 *72/73

Ex.(I) = (3420 *72)/73

Ex.(I) = 3373.15 ID

Ex-23: A difference between commercial interest and exact interest is 1035 ID, find the Com. (I) & Ex.(I)? Sol.

Com.(I) =73 *Diff

Com.(I) =73 *1035

Com.(I) =75555 ID

Ex.(I) = 72 *Diff

Ex.(I) = 72 *1035

Ex.(I) = 74520 ID

Ex-24: Find the commercial interest and exact interest,

if you know that the difference between them is 4197 ID? Sol.

Com.(I) = 73 *Diff Com.(I) = 73 * 4197

Com.(I) = 306381 ID Ex.(I) = 72 *Diff Ex.(I) = 72 * 4197 Ex.(I) = 302184ID

10- The Numbers Method:

The banks usually have many deals with many corporates and individuals every day or week or month; deposit, investment or withdraw.

In this case they make current accounts with the same rate of interest for corporate or individual, to facilities and accuracy the calculation of the bank activates.

The numbers method used for several amounts with different periods at same rate of interest, also it's called (Table method).

To calculate the sums by this way, we must make some steps:

Principal	Number of periods	No.
XXX	Days or	XXX
Xxx	months Days or	XXX
$\Sigma P = xxx$	months	Σ No. = xxx

1 – Make a table:

- 2 Calculate the summation of principals.
- 3 Multiple every principal by it period; to find the No.
- 4 Calculate the summation of No.

5 – Apply the suitable formula.

 $\Sigma I = \Sigma \text{ No. } *(1/12 \text{ or } 360) *(r/100)$

For more explain, let's take some example :

Ex-25: Find the interest in sums at 14%

1500 ID for 30 days

2500 ID for 50 days

4000 ID for 70 days

Sol.

Р	Ν	No.
1500	30	45000
2500	50	125000
4000	70	280000
$\Sigma P = 8000$		Σ No. = 450000

 $\Sigma I = \Sigma No. *(1/360) * (r/100)$

$$\Sigma I = 450000 * (1/360) * (14/100)$$

$$\Sigma I = (450000 * 1 * 14) / (360 * 100)$$

 $\Sigma I = 630000/36000$

∑ I = 175 ID

Ex-26: A merchant want to invest sums at 9%

10500 ID for 5 months

13000 ID for 7 months

16250 ID for 8 months

19400 ID for 11 months

26

Find the total amount?

Sol.

Р	Ν	No.
10500	5	52500
13000	7	91000
16250	8	130000
19400	11	213400
$\Sigma P = 59150$		Σ No. = 486900

- $\sum I = \sum No. *(1/12) * (r/100)$
- $\Sigma I = 486900 * (1/12) * (9/100)$
- Σ I = (486900 *1 *9)/(12 *100)
- $\sum I = 4382100/1200$
- ∑ I = 3651.75 ID
- A =∑ P + ∑ I
- A = 59150 + 3651.75
- A = 62801.75 ID

Ex-27: Baghdad company want to be investing their sums in Cihan bank:

120000 ID on 1st May 2016

136000 ID on 12th June 2016

145000 ID on 17th July 2016

All of sums investing end on 21st September 2016 at 13%, find the commercial interest?

 $1st May \rightarrow 21st Sep. = 143 days$ $12th June \rightarrow 21st Sep. = 101 days$

17th July → 21st Sep. = 66 days

Р	N / days	No.
120000	143	17160000
136000	101	13736000
145000	66	9570000
$\Sigma P = 401000$		Σ No. = 40466000

 $\sum Com. (l) = \sum No. *(1/360) * (r/100)$

 $\Sigma I = 40466000 * (1/360) * (13/100)$

 $\Sigma I = (40466000 *1 *13)/(360 *100)$

 $\Sigma I = 526058000/36000$

 $\Sigma I = 14612.72 ID$

Problems

1- Salar invested 10000 \$ in a saving bank account that earned 2% simple interest.

Find the interest earned if the amount was kept in the bank for 4 years.

2- Ryan borrowed 15000\$ from a bank to buy a car at 10% simple interest. If he paid 9000\$ as interest while clearing the loan.

Find the time for which the loan was given.

3- In how much time will the simple interest on 3500\$ at the rate of 9%, be the same as simple interest on 4000\$ at 10.5%, for 4 years?

4- Ian deposit 3000\$ in State bank of India for 3 years which earn him an interest of 8%.

What is the amount he gets after 1 year, 2 years, and 3 years?

5- Kamal deposited 10000, for 4 years at a rate of 6%.

Find the interest and amount Kamal got.

6- Tim invested 1500\$ at the rate of 6%, for 7 years and 3 months.

Find the amount he got back.

7- Ahmed requests a 2-years loan of 6500\$ from Cihan bank. The bank approves the loan at an annual rate of 14%:

- (i) What is the simple interest of the loan?
- (ii) What is the maturity value of the loan?

8- A student borrows 600 \$ to buy a camera. The loan is over two years, and the simple interest rate is 6% per year. How much interest does the student pay? What is the total amount of money repaid?

9- An investor lent 12000 \$ to a business associate for 6 months at an interest rate of 8% per year. Calculate the interest the investor earns and how much in total will be repaid?

10- Find the exact and ordinary simple interest on a 60-day loan of 1950 \$ at 13.5 %

11- A loan made a loan 100\$ to be repaid with 120 \$ at the end of one month. What was the annual interest rate?

12- How long will it take 5000 \$ to earn 60 \$ interest at 6%?

13- How long will take 1000 \$?

(i) To earn 100 \$ at 15% simple interest?

(ii) To calculate to 1270 \$ at 13.5% simple interest?

14- Find the accumulated value (using both ordinary & exact simple interest)

(i) 500 \$ at 11% over 60 days.

(ii) 1000 \$ at 15% over 150 days.

15- What principal will accumulate to:

(i) 5100 \$ in 6 months at 9% simple interest?

(ii) 580 \$ in 120 days at 18% exact interest?

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16 – A deposit of 1500 \$ is made into a fund–on March (18). The fund earns simple interest at 5% on August (5), the interest rate changes to 4.5%, how much is in the fund on October (23)?

17- A sum of 42000\$ is invested from May (18) ,2006 to April (8) ,2007, at 4.5% simple interest. What amount must he repay in 7 months?

Chapter Two

Commercial discount with simple interest.

1- The concept of trade discount.

The debtor may need cash, so he resorts to collecting and discounting the commercial papers he owns, and then presents them, to the bank before its due date, the bank makes a discount by subtracting the interest amount resulting from the period, the interval between the discount date and the maturity date of the commercial paper is *the nominal value of the commercial paper*. The remaining value is provided to its holder, which is the current value of the paper.

2- Definition of trade discount.

It is the bank's interest in the process of converting the value of a commercial paper into cash before its maturity date. It is a process that allows the ownership of a commercial paper to be exchanged, thus making the bank the beneficiary of the nominal value (the amount of the paper). The bank keeps the amount of the nominal value and provides the holder of the paper with an amount (the current value), before its maturity date.

<u>3-Trade discount account.</u>

The trade discount is calculated based on the nominal value of the commercial paper, at a specific rate of the bank's tip is called the discount rate, and the discount period (n), which is the period between the maturity date of the paper and the discount date. There are two ways to calculate the trade discount.

The normal Method:

EC=(C*r*n)/36000

Where

C= The face value of the paper

r= Discount rate

n=Discount period.

The Constant denominator method:

EC=N/D

Where

N=C*n * D =36000/r

Ex-1: On 13/4/2020, I submitted a commercial paper for discount, with a nominal value of 20,000, due on 30/6/2020, at the bank, to which the discount rate of 5 % was applied. Calculate the discount amount.

Sol:

n= (30-13) +31 +30 =78 days

EC= (C *r*n)/36000

EC= (20000 *5 *78)/36000

EC =216.66 ID

EX-2: What is the nominal value of a commercial bond that was discounted 66 days before its maturity date at a discount rate of 6%, and the discount amount was 550 ID.

Sol:

EC = (C *r *n)/36000

550 = (C *6 *66)/36000

C=(EC*36000)/(r*n)

C = (550 * 36000) / (6 * 66)

C= 50000 ID

EX-3: In22/3/2020. An institution sold a commodity for the amount of 58,500 ID, and the debt was recognized after postponing it with a commercial paper due for payment in25/5/2020, but the holder of the paper needed money, so he approached the bank to negotiate the paper before its maturity date, so the amount of 520 ID was deducted from him at a rate of 10%.

Required is to find the discount date.

Sol:

EC = (C *r *n)/36000

n= (EC *36000)/ (C *r) = (520 *36000)/(58500 *10) = 32 days

The deducted date is 23/4/2020.

EX-4: On 3/7/2020 a paper with a nominal value of 48,000 was negotiated with a bank, and its maturity date was 30/11/2020. The bank received interest from the transaction in the amount of 1,400. Calculate the discount rate.

Sol:

EC = (C *r *n)/36000 1400= (48000 *r * 150)/ 36000 1400 = (4 * r *50) r= 1400/200 =7 %

4-Current value of a commercial paper

It is the value of the amount that the owner of the commercial paper gets when deducting it, and we symbolize it with the symbol V.

There are two methods to calculate the current value.

(i) The normal Method:

V = C - EC = C- (C *r *n)/36000

= C (1- (r*n /36000)

(ii) The Constant denominator method:

V = C - ((C * n)/D) = C ((D-n)/D)

EX-5: Calculate the current value of a commercial paper with a nominal value of 20,000 ID, presented for discount at a bank 60 days before its maturity date at a rate of 6%.

Sol:

V = C (1- ((r *n)/36000) = 20000 (1- ((6 *60) / 36000) = 19800 ID

EX-6: A merchant presented a commercial paper for discount at a bank 4 months before its maturity. If you know that the bank applies a discount rate of 6% ,and the value that the merchant gets after the discount process is 83,300. Calculate the face value of the paper.

Sol:

V = C - ((C *r *n)/1200) 83300 =C (1-(r *n)/1200)) 83300n= C (1- (6 *4)/1200)) 83300 = C (49/50)

C= 85000 ID

EX-7: A commercial paper with a nominal value of 60,000, due for payment on 12/30/2017, presented for discount at a bank n days before its maturity date, at a discount rate of 6%. If you know that its holder may obtain a value of 59,400, specify the discount date.

Sol:

V = C – ((C *r *n)/36000) 59400 =60000 (1- (6*n)/36000) 59400 =10 (6000-n)

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59400 =60000-10n 10n=60000-59400=600 n=60 days

5-Rational (Correct) Discount

It is the discount that is calculated on the basis of real data, specifically on the basis of the current rational value of the commercial paper, which we symbolize with the symbol (V^{\wedge}) and not on the basis of the nominal value, which we symbolize with the symbol (ER). The rational discount is calculated.

ER = $(V^{\wedge} *r *n)/36000$

Where ER = the rational (correct) discount.

V[^] =The current rational value of the commercial paper .

 $V^{\wedge} = C - ER = C - ((V^{\wedge} *r *n)/3 6000)$

 V^{\wedge} + ((V^{\wedge} *r *n)/3 6000) =C

 $V^{\wedge} = C / (1 + (r * n)/3 6000) = (36000 * C) / (36000 + (r * n))$

For the discount correct,

calculate the following formula:

 $ER = C - V^{\wedge} = C - ((36000 * C) / (36000 + (r * n)))$

ER = (C * r *n) / (36000 + (r *n))

EX-8

Commercial paper with a nominal value of 70,000 ID, negotiated 42 days before the maturity date, at a discount rate of 7.5 %.

Find:

Calculate the trade discount. (EC)

The correct discount (ER)

current value (V)

Rational present value (V[^])

Sol:

the trade discounts.

EC = (C * r * n) / (36000) = (70000 * 7.5 * 42)/36000 = 612.5 ID

The correct discount

ER = (C * r * n) / (36000 + (r * n)) = (70000 * 7.5 * 42) / (36000 + (7.5 * 42))

= 607.18 ID

current value

V=C - EC = 70000 - 612.5 = 69387.5 ID

Rational present value

V[^] = C- ER = 70000 -607.18 = 69392.82 ID

EX-9

Commercial paper with a nominal value of 90,000 ID, negotiated 4 months before the maturity date, at a discount rate of 8.5 %.

Find:

(i) -Calculate the trade discount.

(ii)-The correct discount

(iii)-current value

(iv)-Rational present value

Sol:

- (i) Trade discount EC
 EC= (C *r *n) /1200
 EC=(90000 *8.5 *4)/1200
 EC= 2550 ID
- (ii) The correct discount ER ER = (C *r *n)/(1200 + (r *n))ER = (90000 *8.5 *4) (1200 + (8.5 *4))ER = 3060000/1234ER= 2479.74 ID
- (iii) Current value V V= C-EC = 90000-2550= 87450 ID
- (iv) Rational present value V^ V^=C-ER =90000- 2479.74=87520.26 ID

Problems

1-If you know that the difference between the commercial discount and the rational discount is 45.454 dinars, and their ratio is 12/11 required

(i) -Calculate both commercial and rational discount

(ii)- Calculating the nominal value of the debt.

2-A commercial paper with a nominal value of 34,500, which matures after 45 days at an estimated rate of 8%.

Find the discount value.

3-A commercial paper with a value of 15,000, maturity date 20/6/2020, presented for commercial discount on 5/6/2020, at a discount rate of 8%

Required:

(i)-Calculate the number of days of discount.

(ii)-Calculate the discount amount.

4- What is the nominal value of a commercial bond that was discounted 70 days before its maturity date at a discount rate of 8%, and the discount amount was 750 ID.

5- Calculate the current value of a commercial paper with a nominal value of 40,000 ID, presented for discount at a bank 30 days before its maturity date at a rate of 7%.

6- Commercial paper with a nominal value of 70,000 ID, negotiated 3 months before the maturity date, at a discount rate of 7.5 %.

Find:

(i) -Calculate the trade discount.

(ii)-The correct discount

(iii)-current value

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(iv)-Rational present value

7- Commercial paper with a nominal value of 100,000 ID, negotiated 45 days before the maturity date, at a discount rate of 8 %.

Find:

Calculate the trade discount. (EC) The correct discount (ER) current value (V) Rational present value (V^)

Chapter Three

Compound Interest

1- Compound Interest

Compounding means that interest calculated not only on the initial investment but also on the interest of previous period .

In the compound interest the money growth faster than investment in simple interest.

The compound interest may be compounded either:

1-annually (once a year)
2-half- year (semiannually) (twice a year)
3-quartery year (4 times a year)
4-monthly (12 times a year)
5- weekly (52 times a year)
6- daily (365 times a year)

When computing compound interest, the first thing to do is find what is called the *period interest rate (PIR)*

The

PIR = yearly interest rate or r = R/n

Number of interest per year

To find the PIR when interest is compounded

yearly : divide the yearly interest rate by 1.

daily := = = = = = = 365.

Ex-1: Find the period interest rate (PIR) if the annual interest rate is 8% and the interest is compounded quarterly.

Sol:

If the interest is compounded quarterly, then the number of interest payments per year is 4, Bence

PIR = (8%)/4 = 0.08/4 = 0.02 = 2%

The next example shows the difference between simple & compound interest

Ex-2: Find the amount of the

(i) Simple interest

(ii) The compound interests

On a 2000 \$ investment as an annual rate of 4% for 3 years .

Sol:

For simple interest, use the formula

I = P*r*n, when P=2000, r=4%, n=3

I =2000 *0.04 *3 =240 \$

For compound interest, the calculations need to be done three times , one for each year .

For year 1

I =P *r *n = 2000 \$ *0.04 * 1 = 80 \$

During the second year, the 80\$ interest also generates interest, and so the principal is

2000\$ +80 \$ =2080 \$

For year 2

I = P *r *n = 2080 \$ *0.04 * 1 = 83.20 \$

For year 3:

The principal is 2080 \$ +83.20 \$ = 2163.20 \$

Hence:

I = 2163.20 \$ *0.04 *1 = 86.53 \$

Hence the total compound interest is

80\$ +83.20\$ +86.53 \$ =249.73 \$

The total a mount of the investment is

2000\$ +249.73 \$ =2249.73 \$

If interest is compounded half yearly, the same problem would require six calculations. if interest is compounded quarterly, the problem would require 12 calculation and so on .

The following formula can be used :

FV =S =P (1+r)ⁿ

Where:

FV (S) =Future value (a mount)

P = Principal

r=period interest rate, r=PIR

n=number of periods per year times the number of years

Ex-3:

Find the future value and compound interest on 2000 \$ investment at a rate 4% compounded yearly for 3 years .

Sol:

To this case , the period interest rate is 4% since the interest is compounded yearly and n=1*3=3

FV =P (1 +r)ⁿ = 2000 \$ (1+0.04)³

= 2249.73 \$

The amount of the compound interest is

I =FV -P = 2249.73 \$-2000\$ = 249.73 \$

EX-4

Find the future value and compound interest on a 6000 $\$ investment at 10 % compounded half-yearly for 6 years .

Sol:

The period investment rate is (10% / 2) = 0.05 or 5%

The number of periods is 2 *6 =12

 $FV = P (1+r)^n$

- = 6000 (1+ 0.05)¹²
- = 10775.14 \$

The amount of the compound interest is

10775.14\$ -6000\$ = 4775.14\$

Ex-5:

Find the future value ad compound interest on a 500 \$ investment at 6% compounded daily for 5 years .

Sol :

The PIR =(6%)/365 .the number of periods is 365 *5 = 1825

 $FV = P (1+r)^n$

```
= 500 $ (1 +( 0.06 /365 )) <sup>1825</sup>
```

=674.91 \$

The compounded interest is 674.91 \$ - 500\$ = 174.91 \$

EX-6

A person invested \$75000 for a period of 3 years at an annual compound interest rate of 7%. Calculate the interest value for each year.

Sol:

 $I_1 = P^* n * r = 75000 * 1 * (7/100) = 5250 ID$ $I_2 = (75000 + 5250) (7/100) = 80250 * (7/100) = 5617.5 ID$ $I_3 = (80250 + 5617.5) * (7/100) = 85867.5 * (7/100) = 6010.725$

EX-7

A man invested \$12,000 in a bank that offers compound interest at a rate of 4% every three months. What is the value obtained after two years?

Sol:

 $A = P (1+r)^n = P (1+0.04)^8 = 12000 * (1+0.04)^8$

A = 12000 * 1.368569 = 16422.82 ID

Note: Numbers are taken up to six digits after the comma.

EX-8

A person invested a certain amount for 4 years at an annual compound interest rate of 8%, and he obtained an amount of 1,360,489 at the end of the investment period. Calculate the amount invested.

Sol:

A = P (1+r) ⁿ

P=A (1+r)⁻ⁿ = 1360.489 (1+0.08)⁻⁴

 $(1.0.8)^{-4} = 0.735029$

P = 1360.489 * 0.735029 = 1000 ID

EX-9

An amount of 72,800 ID was invested for a period of 6 years with compound interest, to produce a value obtained at the end of the investment of 125491.9848 ID. Calculate the investment rate.

Sol:

EX-10

A person invested an amount of 2,000 ID at a compound interest rate of 6% for a certain period. At the end of the period, he obtained an amount of 2,676,452 ID. Calculate the investment period.

Sol:

A= P (1+r)ⁿ

 $(1+r)^n = A/P = (2676.452)/2000$

 $(1+r)^n = 1.338226$

n=5 years

EX-11

A person deposited an amount of 98,200 ID in a commercial bank at an annual interest rate of 8.5 % for a period of 7 years

Required :

1- The interest earned at the end of the first year of deposit

2-Interest earned at the end of the fifth year only

3- The amount obtained at the end of the period

Sol:

1- I₁ = P *r *n = 98200 *1 * (8.5/100) = 8347 ID

2- $I_5 = A4 * r = P (1+r)^4 * r = 98200 (1 + 0.085)^4 * 0.085$

= 98200 (1.085)⁴ * 0.085 = 11567.76257 ID

3- An = P (1+r)ⁿ
A7 = 98200 (1+0.085)⁷ = 98200 (1.085)⁷ = 173827.9687 ID

The following steps will help you calculate the formula $FV = P (1 + r)^n$

- 1- Enter the value for P
- 2- Press *
- 3- Press (
- 4- Enter 1
- 5- Press +
- 6- Enter PIR
- 7- Press)
- 8- Press the exponent key $(x, \Lambda \text{ or } y x \dots)$

9- Find the value of the number of period.

2-Effective Rate of Interest :

When the interest is compounded more than once a year . it is sometimes necessary to determine an equivalent simple interest rate .

For example , suppose a person invested 800 \$ in a saving account for 1 year at a rate of 8% compounded quarterly .

The future value would be

FV = P (1+r)ⁿ = 800 \$ (1 + (0.08/4)) 1*4 = 865.95 \$

The total interest is 865.95 \$ - 800 \$ = 65.95 \$

Now the comparable simple interest rate is

R = I/(P * n) = 65.95 (800 * 1) = 0.0824 or 8.24 %

In other words , if a person invested 800 \$ in saving account paying 8.24 % simple interest for 1 year , he or she would receive 65.95 \$ in interest , which is the same amount as the person investing 800 \$ for year at 8 % compounded quarterly .

<u>3-The actual interest on simple interest rate that is equivalent to</u> <u>compound interest rate is called the effective rate</u>.

For the loan, this rate is called the annual percentage rate APR.

The following formula can be used for calculating the effective rate

 $E = (1 + r)^n - 1$ where:

E =effective rate

r = period interest rate R/n & n=the number of periods .

Ex-12:

Find the effective rate of interest that is equivalent to a 5% rate compounded

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```
Semiannually (half yearly)
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Sol:

Since the interest is compounded half yearly

R=R/n = 0.05/2 = 0.025

 $E= (1 + r)^n - 1 = (1 + 0.025)^2 - 1 = 0.0506 \text{ or } 5.06\%$

4-Depreciation:

Businesses most often need to purchase equipment, forint buildings, and other necessary items in order to operate their items are called assets.

The worth of an item most often decreases over the year. This decrease in worth is due to what is collect depreciation.

5-The straight -line method:

EX-13:

A factory machine was purchased for15000\$ and has an estimated lifetime of 5 years. if the scrap value at the end of 5 years is estimated of 3000 \$, find the amount of the depreciation for each year.

Sol:

Find the depreciation amount (DA)

DA =original principle – scarp value = 15000\$ -3000 \$ =12000 \$

Divide the depreciation amount by the estimated lifetime.

12000\$ /5 = 2400 \$ per yar

In other words, the value of the machine depreciates 2400\$ per year.

EX-14:

Find the book value (the value of an item often depreciation is calculated) at the end of 4 years of a digital (video camera costing 2400\$ with an expected lifetime of 6 years. the scrap value at the end of lifetime is 3000 \$.

Sol:

DA =2400\$ - 3000\$ =2100 \$

2100 \$ /6 =3500 \$

The amount of depreciation at the end of 4 years is

3500 \$ *4 =14000 \$

The book value of the camera at the end of 4 years is :

24000 \$ - 14000 \$ =10000 \$

6-The Constant -Percentage Method:

Ex-15:

A car costing 24000 \$ depreciates 25% of its value each year. find the book value at the end of 5 years.

Sol:

B =P(1-r)ⁿ

B =24000 \$ (1-0.25)⁵

= 24000\$ (0.75) ⁵

= 5695.31 \$

EX-16:

Determine the rate of depreciation for the machine costing 40000\$ which is estimated to have a useful lifetime of 5 years and scrap value of 5000\$.

Sol:

B = P(1-r)ⁿ

5000 =40000 (1- r)⁵

 $5000/40000 = (1-r)^5$

(1-r)⁵ =0.125

 $(1-r) = (0.125)^{1/5} = (0.125)^{0.2}$

1-r =0.65975

r=1-0.65975 =0.340246=0.34 = 34 %

Problems

Compound Interest

- 1- Find the future value and compound interest on an investment account of 700 \$, compounded quarterly at 10% for 3 years .
- 2- Mr. Zaki deposited 4000 \$ in a saving account paying 2% interest compounded daily, find the future value of the money and the compound interest he earned at the end of 5 years. And find the effective rates:

(i)-6% compounded quarterly.
(ii)-9% = semiannually.
(iii)-9% = monthly.
(iv) 8% = daily.

- 3- The owner of Dana pharmacy plans to remodel his store in 3 years. he estimates that she will need 15000 \$ for the project. how much should he set aside at 4% interest compounded quarterly to have 15000 \$ in 3 years.
- 4- Mrs Young wants to set aside some money for her daughter's college education. She estimates that in 15 years, her 3-years old daughter's college costs will be about 60000 \$. She can obtain an interest rate of 6.5 % compounded semiannually. How much money should invest now.
- 5- Compute the accumulated value of an annuity of 100 \$ invested at the end of each month for one year at an annual rate of 6%.
- 6- Suppose that Ahmed deposits 1000\$ every 3 months in a saving account which pays 8% annual interest compounded quarterly. How much will Ahmed have in the bank at the end of 5 years?
- 7- XYZ Savings bank pays interest at the rate of 4% annually compounded quarterly. How much money will Suzan have in the bank at the end of 5 years if she deposits 250 \$ at the end of each quarter?
- 8- Find the yearly depreciation of a loan tractor costing 1800 \$. It has an expected lifetime of 5 years and a scrap value of 200 \$. using the straight -line depreciation method.
- 9- How long it will take until your 50000 \$ saving grow to 100000 \$ at 3%?

10-Suppose that Ahmed deposits 2000 \$ every 6 months in a saving account which pays 12 % annual interest compounded half-yearly. How much will Ahmed have in the bank at the end of 8 years. Assuming that Ahmed deposits his money at the beginning of each 6-month period.

11-Ahmed purchases a life insurance policy which has an annual premium of 1500 \$ due at the beginning of the year. if he elects to pay his premium in quarterly installments, how much should he pay at the beginning of each quarter if the interest rate is 10% compounded quarterly.

12-Mr. Smith would like to receive 4000 \$ each quarter for 10 years after he retires. How much money (to nearest dollar) does he have to save in a money market fund which pays at the rate of 8% compounded quarterly.

13-When Suzan's husband died, she became the beneficiary of a 100000 \$ life insurance policy. Instead of taking the money in a lump sum, she elects to receive a monthly stipend over a period of 20 years. If the insurance company pays interest at the rate of 6% compounded monthly, what will her monthly income be?

14- Mark must choose between receiving 50000\$ five years from now or taking a lump sum payment of 30000 \$ today. He assumes he can earn 10% compounded annually if he invests 30000 \$. What is the present value of the 50000 \$ future payment?

15- You can afford monthly payments of 250 \$ into an ordinary account that pays 3.5 % compounded monthly. How long will it be until the account contains 10000 \$ (round to the next-higher month if not exact).

16- A file cabinet costs 700 \$. If it has an expected lifetime of 10 years, find the yearly depreciation using the straight-line method. The scrap value is 100 \$.

17- Mark buys an Audi for 200000 \$. If the car depreciates by 10% per year, what is the value of the car in 10 years?